A naive approach to r₁-value calculation: Variability, friend or Foe?

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Warning!





Simulations can be dangerous in the absence biological understanding





Outline

- Introduction to bias, precision and variability
- Study design and FMD titer determination
- Questions
 - What variables contribute to the variability in virus neutralization titers?
 - How much variability should be expected when estimating r₁values?
 - Will pooled sera from 5 animals give similar r₁-values as the average of the 5 individual sera?
 - How many animals are necessary to reliably estimate r₁-values?









Precision and bias



The effect of bias and precision on epidemiological measurements. The origin (0,0) is considered to be the true value. Values simulated from a precise and valid (unbiased) system (A), an imprecise and valid system (B), a precise and invalid (biased) system (C), and an imprecise and biased system (D).



Fosgate GT, Cohen ND. Epidemiological study design and the advancement of equine health. *Equine Vet J* 2008;40:693-700.



Precision and bias



- The preferential removal or retesting of the large positive values will result in a more precise but potentially biased distribution
- Titers often do not look "too small" – especially since expected to follow a log-normal distribution





Random variation

- Epidemiology operates under the assumption that random variation only appears random because we have not yet identified the causes for its existence
- Sources of variability
 - Biological fluctuations of the true values within an animal that are cyclical (diurnal variations)
 - Temporal trends over time related to changes within the animal
 - Analytical fluctuations in measured values due to imprecision in the method of measurement
- Removal of variation could introduce bias
- Research should embrace the inherent variation as if it is excluded then it will not be possible to identify the causes of the variation
- Diagnostic and research approaches to variation might be different





Data collection

- 4 SAT1 reference strains:
 - BOT/1/06/1, KNP/196/91/1, SAR/9/81/1, ZAM/1/06/1
- 5 cattle infected with each reference strain (20 cattle total)
- 26 SAT1 test viruses for VNT
 - 22 field viruses
 - BOT/2/98/1, KNP/10/03/1, KNP/11/03/1, KNP/3/03/1, KNP/7/03/1, MAL/1/85/1, MOZ/1/02/1, NAM/1/10/1, NAM/272/98/1, NAM/308/98/1, SAR/2/09/1, SAR/2/10/1, SAR/33/00/1, SAR/7/03/1, SAR/8/02/1, SAR/9/03/1, TAN/2/99/1, ZAM/2/93/1, ZIM/11/03/1, ZIM/14/98/1, ZIM/3/03/1, ZIM/3/95/1
 - 4 reference viruses
- 1860 total VNT tests performed
- 3 operators
 - Operator 1 700 tests
 - Operator 2 440 tests
 - Operator 3 720 tests





Design overview







Q1:Titer variability

- What variables contribute to the variability in virus neutralization titers?
- VNT titers log₁₀ transformed
- Variance components analysis performed
 - Random effects using restricted maximum likelihood
 - Main effects only model
 - Evaluated variables operator, animal, reference sera, test virus, virus topotype, (day, serum and virus controls)
- Coefficient of variation calculated sd / mean
 - Independently per operator
 - Calculated only for those combinations where test virus, reference sera, and animal were repeated (variability due to day and operator)





Q1: Titer variability

Variable	Variance estimate	Variance percentage	
Test virus	0.051	23.9%	
Topotype	0.010	4.7%	
Animal	0.009	4.2%	
Reference sera	0.008	3.8%	
Operator	0.003	1.4%	
Error	0.132	62.0%	

Design did not allow for sufficient evaluation of day-to-day variation

- Day (testing sequence) did not account for any variability
- Virus and serum controls did not explain overall variability but accounted for all of the operator-associated variability





Q1:Titer variability

Operator	n	Mean (sd) %	Median (range)
1	180	14.1 (10.8)	11.7 (0 – 47.1)
2	20	6.5 (5.8)	3.6 (0.3 – 16.4)
3	180	9.8 (7.6)	8.8 (0 – 36.5)
Overall	380	11.6 (9.5)	9.6 (0 – 47.1)

20-30% coefficient of variation typically considered acceptable for a serological test





Q1:Titer variability







- Operator 1 results might suggest too much variability
- Operator 2 had a small sample size for evaluation





Q2:r₁-value variability

• How much variability should be expected when estimating r₁-values?

- Monte Carlo (MC) simulation procedure sample of 100,000 iterations
- Randomly selected titer values
 - Reference titer (homologous) (1-4)
 - Test virus (heterologous) (1-26; included homologous)
- Individual r₁-value calculated at each iteration
- Description of r₁-values
 - Point estimate median of MC sample
 - 95% CI percentiles of MC sample
 - Probability function
 - 1 cumulative probability





Q2:r₁-variability results

Reference serum	Test virus	Median [95% CI]	Pr >0.3	Pr >0.5	Pr >0.7
ZAM/1/06	SAR/9/03/1	0.25 [0.01, 5.49]	0.429	0.306	0.233
BOT/1/06	ZAM/1/06/1	0.25 [0.02, 3.02]	0.475	0.329	0.227
BOT/1/06	SAR/7/03/1	0.25 [0.02, 4.47]	0.448	0.315	0.231
BOT/1/06	NAM/272/98/1	0.25 [0.04, 1.26]	0.385	0.216	0.103
SAR/9/81	KNP/10/03/1	0.25 [0.04, 1.95]	0.452	0.283	0.191
SAR/9/81	BOT/1/06/1	0.25 [0.05, 1.35]	0.412	0.214	0.101
BOT/1/06	TAN/2/99/1	0.25 [0.05, 1.62]	0.499	0.334	0.170
KNP/196/91	BOT/1/06/1	0.25 [0.05, 3.16]	0.469	0.304	0.216
ZAM/1/06	KNP/196/91/1	0.25 [0.05, 5.89]	0.467	0.345	0.265



















Q3:Pooled vs individual

- Will pooled sera from 5 animals give similar r₁-values as the average of the 5 individual sera?
- Monte Carlo simulation procedure sample of 100,000 iterations
- Randomly selected titer values
 - Reference titer (homologous) (1-4)
 - Test virus (heterologous) (1-26; included homologous)
- Individual r₁-values calculated
- Pooled r₁-values calculated from pooled titers corresponding to the randomly selected individual titers
- Descriptive evaluation for differences in r₁-values
 - Point estimate median of MC sample
 - Compared to individual and pool r₁-values calculated by an experienced diagnostician







Reference sera SAR/9/81



Test virus



r₁-value



Q3:Pooled results



Reference sera KNP/196/91







Q3:Vaccine match(?)







Q4:Number of animals

- How many animals are necessary to reliably estimate r₁-values?
- r₁-values calculated from the entire dataset using the mean values over all operators and animals were considered the true r₁-values
- A sample of 20,000 MC iterations were performed
- Possible samples sizes from 1-15 evaluated
- Reference sera titers randomly selected
- Test virus titers randomly selected
- r₁-value calculated as Mean (test virus) / Mean (ref sera) titers
- Bias calculated as Sample r₁-value GS r₁-value
- Bias% calculated as Bias / GS r₁-value * 100
- Means used as point estimates with variability evaluated by percentiles of MC iterations









• Mean percentage and 97.5% upper limit for MC bias









• Mean percentage and 97.5% upper limit for MC bias





Conclusions

- Preferential re-testing of high positive titers could introduce bias in r₁-value determination
- VNT repeatability is acceptable and operator accounts for minimal variability
- There is substantial variability due to virus within topotypes
- A single r₁-value point estimate might be sufficient without a measure of variability
- r₁-value calculation method could affect determination of the best vaccine match
- Sample size of 5-6 is reasonable for r₁ value estimation



